

# Navier–Stokes Computations and Experimental Comparisons for Multielement Airfoil Configurations

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A two-dimensional unstructured Navier–Stokes code is utilized for computing the flow around multielement airfoil configurations. Comparisons are shown for a landing configuration with an advanced-technology flap. Grid convergence studies are conducted to assess inaccuracies caused by inadequate grid resolution. Although adequate resolution is obtained for determining the pressure distributions, further refinement is needed to sufficiently resolve the velocity profiles at high angles of attack. For the advanced flap configuration, comparisons of pressure distributions and lift are made with experimental data. Here, two flap riggings and two Reynolds numbers are considered. In general, the trends caused by variations in these quantities are well predicted by the computations, although the angle of attack for maximum lift is overpredicted.

## Nomenclature

$b$	= span of wind-tunnel model
$C_l$	= lift coefficient
$C_p$	= pressure coefficient
$c$	= reference chord taken to be the chord of the undeflected airfoil
$M_\infty$	= freestream Mach number
$q$	= magnitude of velocity
$q_\infty$	= magnitude of velocity in freestream
$Re$	= Reynolds number
$u$	= velocity component in direction of surface-tangent vector
$x, y, z$	= Cartesian coordinates
$y^+$	= turbulent boundary-layer parameter
$\alpha$	= angle of attack
$\eta$	= chordwise location on airfoil (referenced to undeflected position)

## Introduction

THE goal of a high-lift system is to generate as much lift as possible without separating the flow.<sup>1</sup> Without external devices such as wall suction, the most effective way to achieve this goal is through the use of multiple elements to manipulate the inviscid pressure distribution to reduce the pressure rise over each element.<sup>1,2</sup> However, the presence of multiple elements seriously complicates analysis procedures because of important and often complex interactions between the individual elements. While inviscid analysis can be accomplished in minutes with panel methods or unstructured-grid Euler solvers, it is necessary to use viscous techniques to accurately predict the flows about these configurations. The reason for this is that although the tailoring of the flowfield to prevent separation is largely achieved through circulation interactions between the elements, many viscous effects can

have large influences on the pressure distributions. While these include obvious effects such as displacement thickness and separation on the surfaces, wake interactions between forward and aft elements as well as flow reversal off the surface can contribute significantly in determining the overall performance of the high-lift system.<sup>3–5</sup>

For computations on multielement airfoils, unstructured grid methods may offer a good alternative to more traditional methods of analysis. This is due in part to the decreased time required to generate grids over complicated geometries. Also, unstructured grids offer the potential to adapt the grid to improve the accuracy of the computation without incurring the penalties associated with global refinement. However, despite the advantages of unstructured grids, they are typically much slower than structured grid solvers. Also, the ability to obtain solutions through local adaptation that are comparable to those obtained through global refinement remains an area where further work is required.<sup>6</sup> Although further work remains to fully realize their potential, much progress has been reported in computing viscous flows on unstructured grids.<sup>7–10</sup>

The purpose of this study is to present computational results obtained with a particular unstructured grid method<sup>11</sup> that has been applied to several flows over multielement airfoils. Comparisons between computational results and experimental data are made to assess the effectiveness of the present code, to aid in determining future directions, and to provide useful comparisons for other researchers working in this field.

## Computational Method

The computational method used in this study is a node-based, implicit, unstructured, upwind flow solver described in Ref. 11. In this code, the discretization of the convective and viscous terms is handled similarly to the method of Ref. 8. The inviscid fluxes are obtained using Roe's approximate Riemann solver<sup>12</sup>; the viscous terms are evaluated with a Galerkin-type approximation that results in a central-difference formulation for these terms. Two different turbulence models are presently utilized in the code. These include both the Baldwin–Barth<sup>13</sup> model and the Spalart–Allmaras<sup>14</sup> model. At each time step, the equation for the turbulent viscosity is solved separately from the flow equations, which results in a loosely coupled solution process that allows for a relatively easy interchange of other turbulence models. Although both turbulence models have been used extensively with good success, the present study reports only results obtained with the Spalart–Allmaras model. This is due to both space limitations

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and to the improved accuracy of this model for free-shear flows, which are important for multielement airfoils due to wake interactions.

### Experimental Data

All of the experimental data used in the present work have been obtained in the Low Turbulence Pressure Tunnel (LTPT) located at the NASA Langley Research Center.<sup>15</sup> The tunnel is a single-return, closed-throat wind tunnel that obtains high Reynolds numbers by operating at pressures up to 10 atm. The test section is 3 ft wide by 7.5 ft high by 7 ft long. Side-wall boundary-layer suction is applied to promote two-dimensional flow.<sup>16</sup>

Lift and moment measurements are obtained by using both a force balance and an integration of surface pressures; drag is obtained from a wake survey using three five-hole probes. The uncertainty of the lift coefficient from the balance measurement is  $\pm 0.074$  at  $Re = 9 \times 10^6$ , but increases to  $\pm 0.13$  at  $Re = 5 \times 10^6$ . The pitching moment uncertainty, as measured by the balance, is  $\pm 0.03$  at  $Re = 9 \times 10^6$ , and  $\pm 0.05$  at  $Re = 5 \times 10^6$ . The lift coefficient is estimated to be within  $\pm 0.02$  when obtained from pressure integration for  $Re = 5$  and  $9 \times 10^6$ . The drag coefficient is estimated to be accurate to within  $\pm 0.001$  for attached flows.<sup>17</sup> Pressure coefficient



Fig. 1 Geometry for three-element airfoil 30P-30AG.

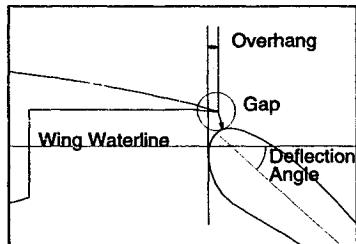


Fig. 2 Definition of gap and overhang for flap.

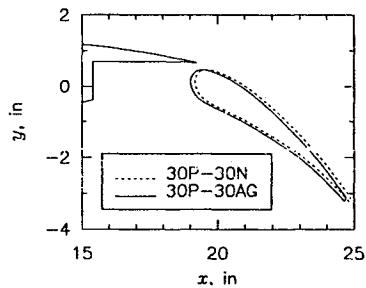


Fig. 3 Differences in flap rigging for the 30P-30N and 30P-30AG configurations.

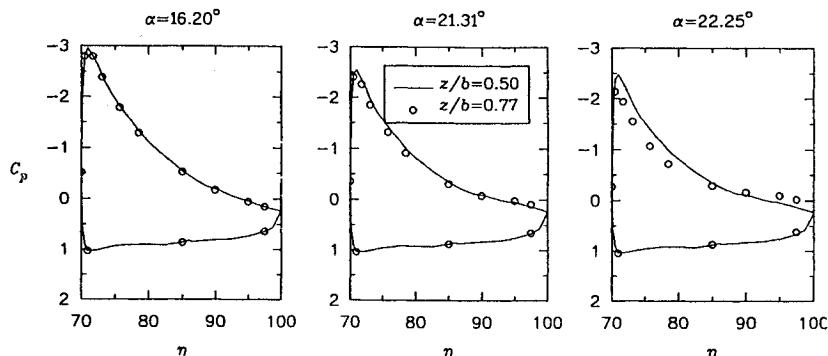


Fig. 4 Experimental pressure distributions at two spanwise locations for several angles of attack.

distributions are obtained from pressure orifices located along the model and are accurate to within  $\pm 0.022$  for  $Re = 9 \times 10^6$  and  $\pm 0.038$  for  $Re = 5 \times 10^6$ .

For the calculations that follow, comparisons will be made with experiments obtained from two different data sets and the presentation of results is organized accordingly. A brief description is given for each data set.

The test data is the result of a cooperative experimental program between the Douglas Aircraft Company and the NASA Langley Research Center and is reported in Refs. 18 and 19. Test Reynolds numbers varied between  $5 \times 10^6$ ,  $9 \times 10^6$ , and  $1.6 \times 10^7$ . The angle of attack included a range of approximately  $-4$  through  $23$  deg. The tests have been conducted without forced boundary-layer transition. The overall geometry, which is shown in Fig. 1, is a three-element configuration based on an 11.55% thick supercritical airfoil. The slat and flap chord ratios are 14.48 and 30%, respectively, based on the airfoil chord for the undeflected position.

For the current study the deflections of both the slat and the flap are set at 30 deg and two different flap riggings are considered. A "rigging" refers to a combination of gap and overhang settings as defined in Fig. 2, and a specific rigging is assigned a letter designation. For the first configuration, denoted as 30P-30N (slat deflection 30 deg, slat rigging P, flap deflection 30 deg, flap rigging N), the flap overhang is 0.25% of the undeflected airfoil and the flap gap is 1.27%. For the second configuration, which is denoted as 30P-30AG, both the gap and overhang are 1%. In Fig. 3, a more detailed view of the flap riggings for the two configurations is shown.

The data for these configurations have been obtained from two separate tunnel entries. Because the first test considered both three- and four-element airfoils, the flap was constructed in two pieces, which were then assembled on site. During these tests, force and moment data were obtained for many flap riggings, including those discussed here. From these experiments, it was found that the 30P-30N configuration exhibited a slightly higher  $C_{l_{max}}$  than did the 30P-30AG. A single-segment flap was then constructed and the 30P-30N geometry was studied in more detail in a subsequent test. During this test, more detailed data, such as velocity profiles, were obtained and are presented in Ref. 19.

To make meaningful interpretations between computational and experiment results, an indication of the two dimensionality of the flowfield is necessary. Figure 4 shows experimental pressure distributions at several angles of attack obtained at two different spanwise locations on the model. The  $z/b = 0.5$  location corresponds to the centerline of the tunnel, which has 146 pressure taps. In order to better assess the two dimensionality of the flow, several pressure taps are also present at  $z/b = 0.77$ , which is approximately midway between the centerline of the model and the wind-tunnel wall. As seen in the figure, excellent two-dimensional flow is maintained at an angle of attack of 16.2 deg. Slight three-dimensional effects are present at 21.31 deg and three dimensionality is clearly indicated at 22.25 deg.

## Results

The results of the comparisons are presented later in this article. For the computations, the Courant–Friedrichs–Lewy (CFL) number has been ramped linearly from 20 to 100 over 100 iterations. The lift coefficient is constant to within about 0.1% of the total lift (fourth significant digit) and the pressure

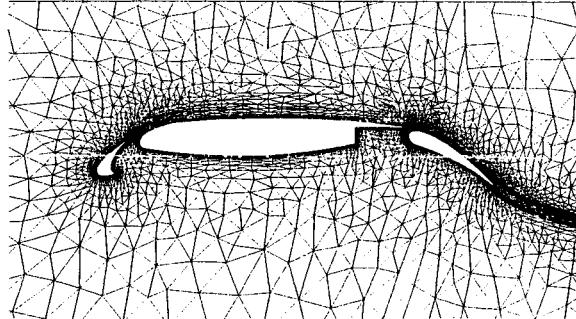


Fig. 5 View of sample unstructured grid for three-element airfoil.

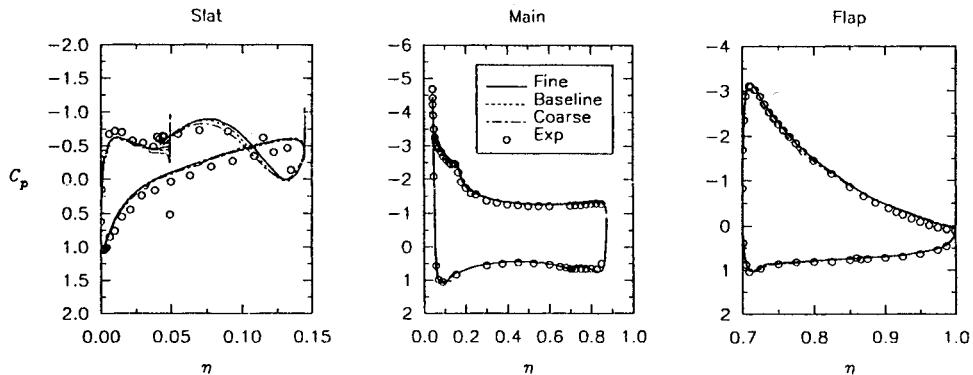


Fig. 6 Computed pressure distributions on the coarse, baseline, and fine grids for 30P-30N with  $M_{\infty} = 0.2$ ,  $Re = 9 \times 10^6$ ,  $\alpha = -0.03$  deg.

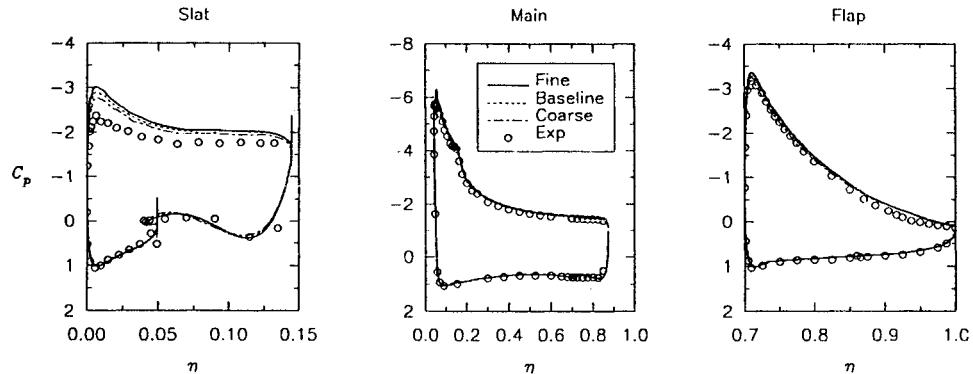


Fig. 7 Computed pressure distributions on the coarse, baseline, and fine grids for 30P-30N with  $M_{\infty} = 0.2$ ,  $Re = 9 \times 10^6$ ,  $\alpha = 8.23$  deg.

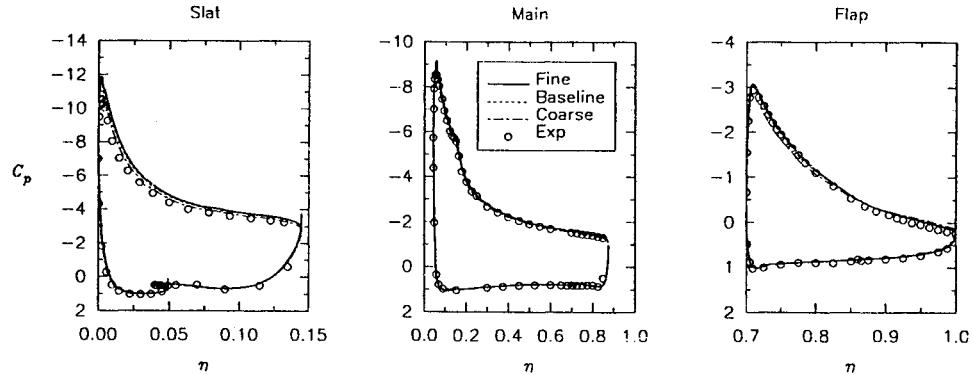


Fig. 8 Computed pressure distributions on the coarse, baseline, and fine grids for 30P-30N with  $M_{\infty} = 0.2$ ,  $Re = 9 \times 10^6$ ,  $\alpha = 16.30$  deg.

distributions and velocity profiles show no differences over 500 iterations when plotted.

All grids used in the present study have been generated using the grid generation procedure described in Ref. 20; a sample is shown in Fig. 5. In this procedure, structured grids are first generated around individual components. These grids are then used to define a cloud of points that is triangulated with a stretched-Delaunay triangulation procedure to establish the connectivity relationships. Although the aspect ratios of the triangles near the surface are generally very large because of the extremely small spacing required at the wall, grids generated in this manner tend to have relatively few cells with large angles that can negatively compromise accuracy.<sup>21</sup> For the grids used here, fewer than 2% of the angles are greater than 120 deg.

Comparisons between computed results and experimental data are presented for the three-element advanced flap configurations (30P-30N and 30P-30AG) discussed earlier. The first set of results is for the 30P-30N configuration at several angles of attack with a Mach number of 0.2 and a Reynolds number of  $9 \times 10^6$ . Simultaneously presented are the results of varying grid densities on computed pressure distributions

and velocity profiles, which are used to ascertain the level of numerical errors in the computations.

For these studies, three grids have been utilized. The first grid, which will be referred to as the coarse grid, consists of 22,491 nodes, 524 of which lie on the surfaces of the elements. The spacing at the wall for this mesh is  $4 \times 10^{-6}$  normalized to the chord length of the airfoil in the undeflected position. This spacing yields a  $y^+$  of less than two for the point next to the wall at the rear of a unit-length flat plate. Finer grids are obtained by simultaneously increasing the number of points

in each direction to obtain as close to a uniform refinement as possible. In the current study, the number of points in each direction is increased with each refinement by a factor of roughly  $\sqrt{2}$  so that the total number of nodes with each refinement is approximately doubled over the previous mesh.

With this procedure, the second mesh in this family of grids contains 49,596 nodes with 806 points on the surfaces. This mesh will be referred to in future discussions as the baseline mesh. For this mesh, the spacing at the wall is about  $2 \times 10^{-6}$  and results in a  $y^+$  of less than one, according to flat

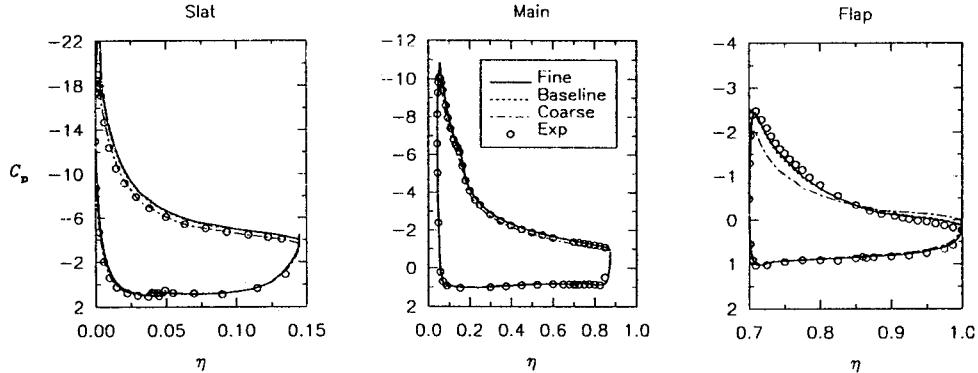


Fig. 9 Computed pressure distributions on the coarse, baseline, and fine grids for 30P-30N with  $M_\infty = 0.2$ ,  $Re = 9 \times 10^6$ ,  $\alpha = 22.36$  deg.

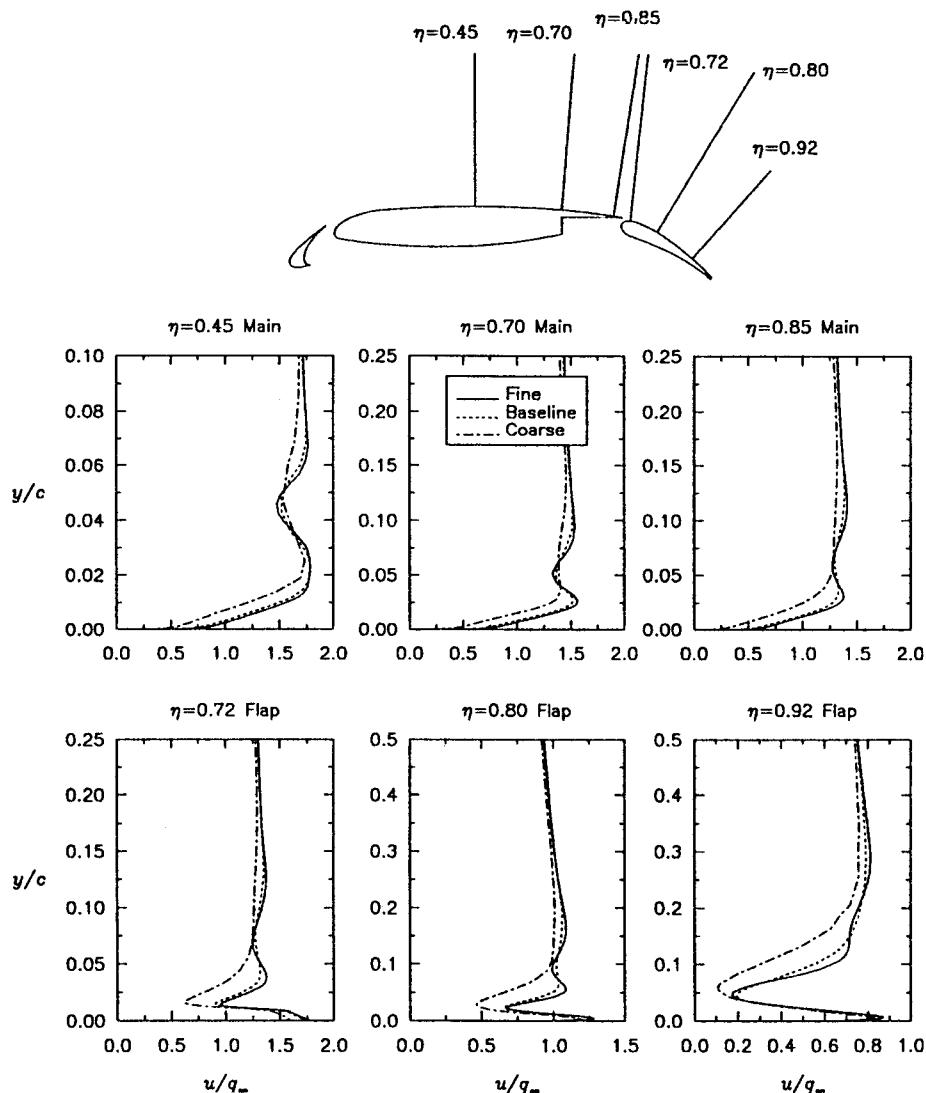


Fig. 10 Computed velocity profiles on the coarse, baseline, and fine grids for 30P-30N with  $M_\infty = 0.2$ ,  $Re = 9 \times 10^6$ ,  $\alpha = 22.36$  deg.

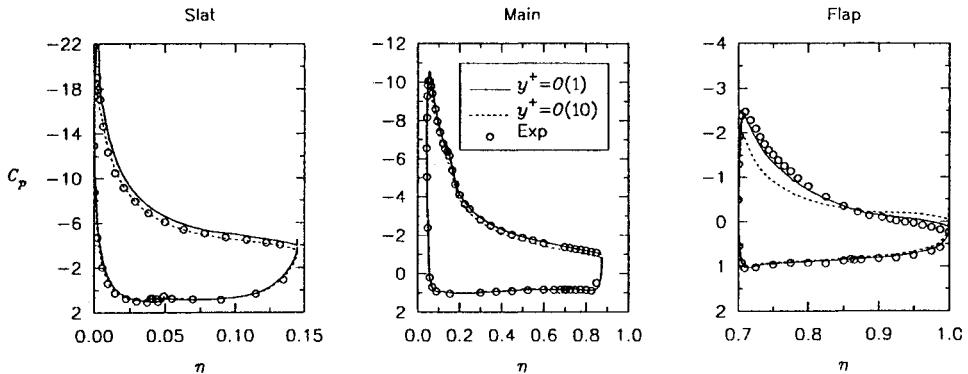


Fig. 11 Comparison of pressure distributions on grids with  $y^+ \approx 1$  and  $y^+ \approx 10$  for 30P-30N with  $M_\infty = 0.2$ ,  $Re = 9 \times 10^6$ ,  $\alpha = 22.36$  deg.

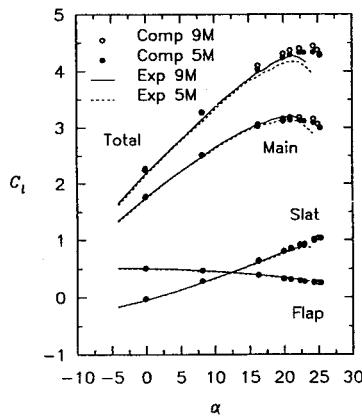


Fig. 12 Experimental and computational lift vs angle of attack for  $Re = 5 \times 10^6$  and  $9 \times 10^6$  for 30P-30N with  $M_\infty = 0.2$ .

plate estimates. In a similar fashion, another finer grid is generated that has 87,783 nodes with 1036 points on the solid surfaces; it is referred to here as the fine grid.

Pressure distributions on all grids are shown in Figs. 6–9 for  $\alpha = -0.03$  deg,  $\alpha = 8.23$ , 16.30, and 22.36 deg, respectively. As seen, the variation in the pressure distribution between the coarse grid and the other two grids is relatively small up to  $\alpha = 22.36$  deg. However, at this angle of attack, the loading on the flap is noticeably less for the coarse grid than for the baseline and fine grids, which continue to yield very similar results. Also, an obvious discrepancy exists in the pressure distribution on the slat for an angle of attack of 8.23 deg. The cause of this is unknown, but could be attributable to a number of sources including wind-tunnel wall corrections or an inaccurate representation of the separated flow under the cove that leads to higher circulation around this element. Although not shown, it is interesting to note that excellent agreement is obtained on the slat, as well as the other elements, when the point vortex correction in the far field for the computations is removed. However, numerical studies for the Euler equations with this same three-element airfoil indicate that the presence of the point vortex significantly decreases the dependence of the solution on the placement of the far-field boundary as expected. Therefore, the improved agreement obtained without the vortex is evidently fortuitous. Note also that the pressure distributions on both the main element and the flap indicate slightly higher lift than the experiment, which could also account for a higher circulation on the slat.

Computed velocity profiles at several locations along the main element and the flap are shown in Fig. 10 for an angle of attack of 22.36 deg. Also shown is an illustration that indicates the locations on each element where the data are obtained. Note that these locations are referenced to the air-

foil coordinates in the undeflected position. Results are shown for this angle of attack because they indicate the most variation between the coarse, baseline, and fine grids. As seen, the agreement between the baseline grid and the fine grid is reasonably good on the main element, but the coarse grid is clearly inaccurate. Furthermore, the trend with grid refinement is to decrease the boundary-layer thickness on the main element. The increased thickness of the boundary layer with the coarse grid is likely to be responsible for the decreased flap loading obtained on this grid and seen in Fig. 9.

On the flap, the major difference between the baseline grid results and the fine grid results is in the enhanced resolution of the slat wake on the finer grid. This wake is very apparent at the station immediately downstream of the main element ( $\eta = 0.72$ ), but quickly dissipates so that its presence is barely detectable at the location towards the back of the flap ( $\eta = 0.92$ ). The difference in profiles between the baseline and fine grids indicates that further refinement is necessary to accurately resolve these details. Although not shown, as the angle of attack is reduced, the difference in the profiles decreases so that the baseline grid and fine grid give essentially identical results at an angle of attack of  $-0.03$  deg.

An additional study of grid effects has been conducted and is presented in Fig. 11. For this study, a grid very similar to the baseline grid has been generated with the spacing of the grid points next to the wall based on obtaining a  $y^+ \approx 10$  instead of  $y^+ \approx 1$ . Note that the spacing is determined based on estimates from a flat plate at the Reynolds number in question ( $Re = 9 \times 10^6$ ). In order to obtain  $y^+ \approx 1$ , the required spacing at the wall is approximately  $2 \times 10^{-6}$ ; however,  $y^+ \approx 10$  allows spacing an order of magnitude larger. Although not shown here, the  $y^+$  obtained from actual computations on the baseline grid at an angle of attack of 22.36 deg is approximately one over the first 20% of the airfoil and then drops to about one-half afterwards. Values of  $y^+$  for the second mesh are slightly above 10 for the first 20% and drop to around 5 for most of the remainder of the element. Because the sublayer for a turbulent boundary layer extends to a  $y^+$  of approximately 10, essentially no points exist in this region over the first 20% of the airfoil for this mesh.

Figure 11 shows that inadequate spacing at the wall drastically affects the pressure distribution on the flap; hence, the other elements are effected as well. Inspection of the velocity profiles (not shown) reveals that inadequate spacing near the wall leads to an artificial thickening of the computed boundary layer on the main element. As discussed in Ref. 3, a thick boundary layer on the main element acts to suppress the loading on the flap. Therefore, the effect of the artificially thickened boundary layer is to artificially suppress the loading on the flap.

Numerical experiments indicate that inadequate wall spacing has little effect on the pressure distributions at lower angles of attack, such as 8.23 deg. It is primarily at higher angles where the wall spacing has been observed to be critical. Note

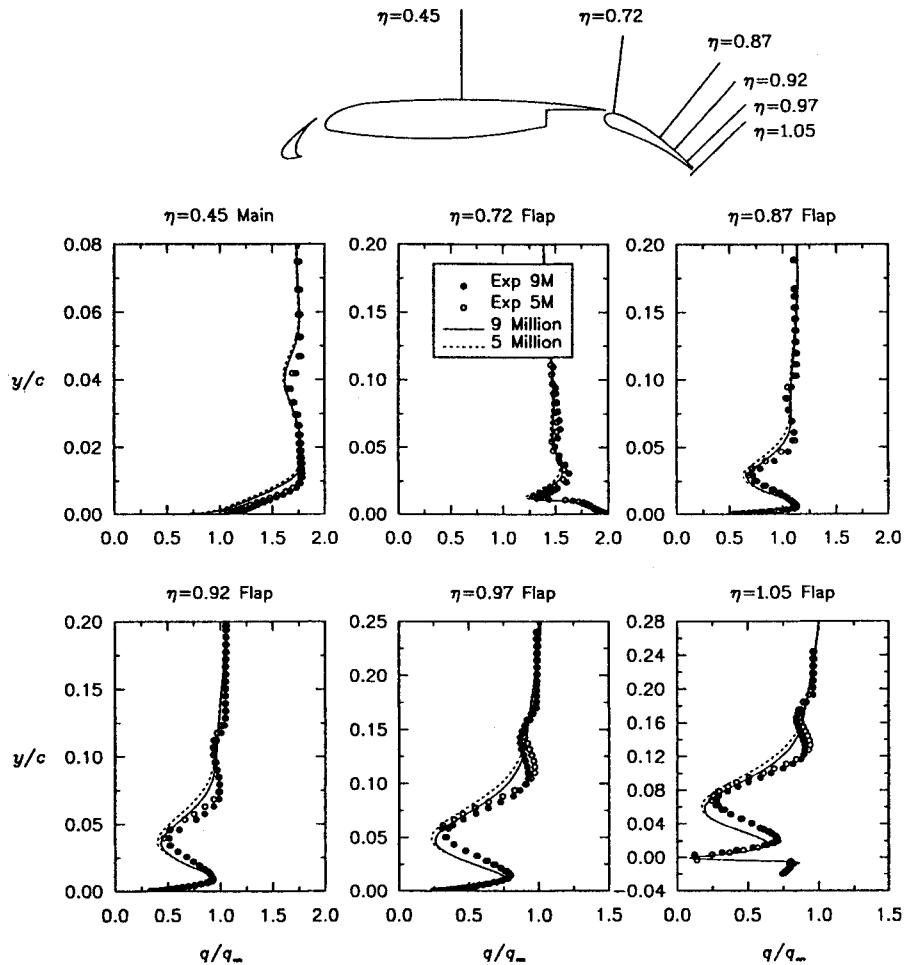


Fig. 13 Comparison of velocity profiles at Reynolds numbers of  $Re = 5$  and  $9 \times 10^6$  for  $30P-30N$  with  $M_\infty = 0.2$ ,  $\alpha = 16.3$  deg.

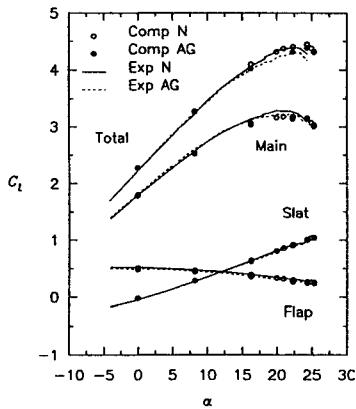


Fig. 14 Comparison of computational and experimental lift for the  $30P-30N$  and  $30P-30AG$  configurations with  $M_\infty = 0.2$ ,  $Re = 9 \times 10^6$ .

that for single element airfoils, the effect of wall spacing is not as dramatic as it is for multielement configurations because the wake does not impinge on aft elements. Also, achieving a  $y^+$  of 1 is not a necessary requirement; typically, values similar to those used for algebraic turbulence models ( $y^+ \approx 3$ ) should be sufficient.<sup>13,14</sup>

A summary of computed and experimental lift coefficients at Reynolds numbers of both 5 and  $9 \times 10^6$  are shown in Fig. 12. Here, the lift vs angle of attack is shown for the full configuration, as well as for the individual elements. The lift for each of the individual elements is obtained from pressure integration and is not corrected for wind-tunnel wall effects.

The total lift, on the other hand, is also computed from pressure integration, but has been corrected for wall interference.

As seen in the figure, the lift agreement is good for the uncorrected data on each element, whereas the total lift (corrected) for the configuration is overpredicted in the computations. Although not shown, improved agreement between the computations and the experiment is obtained by using the lift from the force balance because it is slightly higher. For the computations, the angle of attack for maximum lift is not accurately predicted for either Reynolds number; however, the overall trend is well represented. The experiment and computations both obtain higher lift for a Reynolds number of  $9 \times 10^6$  over that of  $5 \times 10^6$ , and the main element begins to lose lift before either of the other elements.

A comparison of velocity profiles for Reynolds numbers of 5 and  $9 \times 10^6$  are shown in Fig. 13 for  $\alpha = 16.3$  deg. Only small differences are seen over the main element, although the boundary layer at  $9 \times 10^6$  appears to be slightly thinner than at  $5 \times 10^6$ . Over the flap more differences are apparent; the computations at the lower Reynolds number show lower velocities than at a Reynolds number of  $9 \times 10^6$ . Although the results from the grid convergence studies indicate that more refinement is required to adequately resolve the wake emanating from the slat that persists to the back of the flap, the overall trends in the velocity profiles with variations in Reynolds number are well captured.

The last case considered from this data set is a comparison of the computations and experiment between the  $30P-30N$  and the  $30P-30AG$  configurations. Recall from the description of the wind-tunnel tests that these configurations differ only in the flap rigging, as shown in Fig. 3. Because the tests for the  $30P-30AG$  configuration were conducted with only

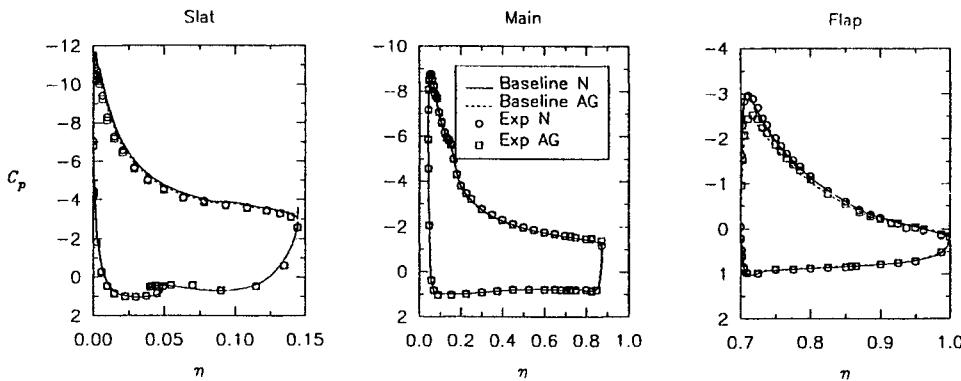


Fig. 15 Comparison of computational and experimental pressure distributions for the 30P-30N and 30P-30AG configurations with  $M_\infty = 0.2$ ,  $Re = 9 \times 10^6$ ,  $\alpha = 16.3$  deg.

the two-segment flap, the data shown next for both the 30P-30N and the 30P-30AG are from this same test.

A comparison of the lift coefficients vs angle of attack for these configurations is shown in Fig. 14 for a Reynolds number of  $9 \times 10^6$ . In both the computations and the experiment the 30P-30N configuration attains higher lift coefficients than the 30P-30AG. Note that the agreement between the computed lift and the experimental data for the 30P-30N configuration is somewhat improved over that shown previously in Fig. 12. This is because the data for the two-segment flap is used for the current figure. Careful inspection of Figs. 12 and 14 indicates that differences in the experimentally obtained lift between the one- and two-segment flap appear to start at about 20 deg. This difference may be due to slight differences in the model geometry or because the flow may no longer be two dimensional at this angle of attack.

A comparison of computed and experimental pressure distributions is shown in Fig. 15 for an angle of attack of 16.3 deg. The agreement between the computations and experiment is good for all elements. Although little difference due to the flap rigging is apparent on the slat and the main element, the flap shows a higher suction peak for the 30P-30N configuration than for 30P-30AG.

### Conclusions and Recommendations

A two-dimensional unstructured Navier-Stokes code has been utilized for computing the flow around multielement airfoil configurations. Comparisons are shown for a landing configuration with an advanced-technology flap for angles of attack up to the maximum-lift condition. A systematic grid convergence study has been conducted to assess the inaccuracies in the computations caused by inadequate grid resolution. Below maximum lift, pressure distributions are adequately resolved by using approximately 50,000 nodes. However, at high angles of attack, further grid refinement is required to obtain suitable levels of grid convergence for velocity profiles. This could be achieved by continuing to refine the mesh in a systematic manner, or possibly through the use of adaptive gridding or higher-order methods. The grid studies further indicate that care must be taken in obtaining accurate resolution of the wall boundary layers on upstream elements by using sufficiently small spacing of grid points. The use of a grid with inadequate wall spacing [ $y^+ = 0(10)$ ] results in an artificially thick boundary layer on the main element that severely effects the loading on the flap and, hence, the entire configuration.

Comparisons for the advanced flap configuration between computed and experimental pressure distributions are made for two flap riggings. In addition, lift coefficients and velocity profiles are compared for Reynolds numbers of 5 and  $9 \times 10^6$ . In general, the trends due to variations in rigging and

Reynolds numbers are predicted well by the computations, although the angle of attack for maximum lift is overpredicted.

### Acknowledgment

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